

# Controlled Publication Master Dossier

Claims register, venue-neutral manuscript, gap audit, canonical operational model specification, and read-only reproducibility guide

**v7.13 FROZEN**

**R1-R3 CLOSED**

**NO SOLVER RERUN**

## Scope statement

The terminal v7.13 result is reported only as a numerical gate classification of the frozen homogeneous model. The package now exposes its operational equations, exact gates, immutable artifacts, and read-only verification route. This does not claim empirical confirmation, independent numerical reproduction, a fundamental covariant action, or ontological proof. AP1-AP3 remain a prospective falsification program.

**30 August 2026 / venue-neutral controlled draft**



# Dossier manifest

This milestone PDF is generated from the authoritative publication-latest source files. The numerical state and recovery files were not modified.

| Document                                               | Role                                      | SHA-256                                                           |
|--------------------------------------------------------|-------------------------------------------|-------------------------------------------------------------------|
| APEIRON_PUBLICATION_CLAIMS_REGISTER_LATEST.md          | German internal claims audit              | ef17d6be90ff1a59de7fbe7a6172c4115a142601512302acf7bd9bf44076ccf6  |
| APEIRON_MANUSCRIPT_LATEST.md                           | English scientific master manuscript      | 4559aa3ee8cfae41407290024084bf706667275b1387a56ee48d7bb727eccc9   |
| APEIRON_PUBLICATION_GAP_REPORT_LATEST.md               | German publication gap report             | d9f9307bcae733444aefafb53144b0c0f0d6a850acea32685903b62a2bfa9909  |
| APEIRON_CANONICAL_MODEL_SPECIFICATION_LATEST.md        | Canonical operational model specification | 9f9fa5454e7e298c7344a240db6672644335302f8459fb59c74c30bb82c897e4  |
| README_REPRODUCIBILITY.md                              | Read-only reproducibility guide           | ffbcbd3cc38a04c1ffaa223f35d9a9b4e097c5847f720ba4c80652b52b2e7530  |
| APEIRON_V7_13_GATE_SPECIFICATION_LATEST.json           | Machine-readable exact v7.13 gate table   | 64e44a228e856814b66c129ce7fe741797b8cbe75756b684c582827bd72f71de  |
| APEIRON_REPRODUCIBILITY_MANIFEST_LATEST.json           | Machine-readable SHA-256 manifest         | eb5475e0f327d340b8f33d1b4b3ea00af9a779a9a4a241a20f886184d44cdec1  |
| APEIRON_PUBLICATION_REPRODUCIBILITY_PACKAGE_LATEST.zip | Tested reproducibility ZIP                | 801f19dc26808184ccf4dfa33dd5429831c42fdbab0b2048d16fd7c50b6ae0ac2 |

## Reading order

Part I fixes the publication claim ceiling. Part II is the venue-neutral manuscript. Part III records remaining gaps. Part IV states the canonical operational model. Part V gives the read-only verification instructions.

## Part I - Controlled claims register

German internal audit and publication-language ceiling

# Apeiron - Publikations-Claims-Register (Latest)

Version: 1.1-red-blockers-closed Stand: 30. August 2026 Sprache: interne Auditdokumentation Deutsch Status: Claims-Freeze aktualisiert; R1-R3 dokumentarisch geschlossen; numerische Linie unverändert

## 1. Zweck und Geltungsbereich

Dieses Register begrenzt die erste venue-neutrale Grundlagenpublikation auf den nachweisbaren Stand. Der terminale v7.13-HARD-PASS, der v6.74-NONPASS-Gegenendpunkt und die Float64-Crossing-Klassifikation bleiben eingefroren. Es wurde kein Solver gestartet, kein Diagnosewert aus den Feldgleichungen neu berechnet und keine Klassifikation wiederholt.

Die neu aufgenommenen technischen Quellen schließen die bisherigen Dokumentationslücken zu operationalen Gleichungen, Freiheitsgraden, Einheiten, v7.13-Gates und Artefaktintegrität. Sie liefern keine fundamentale Wirkung, keine Kontinuumsanalyse, keine Störungstheorie und keine empirische Bestätigung. Anlage A bleibt ein zukünftiges Forschungsprogramm.

## 2. Autoritative Evidenzbasis

| Kürzel | Quelle                                                                                | Verwendbarer Nachweis                                                                       | Integrität / Status                                                               |
|--------|---------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|
| H1     | START_HERE_APEIRON_LATEST.md, Eingangsstand dieses Arbeitsblocks                      | terminaler Stand, Verbote, Resume-Punkt                                                     | Eingangs-SHA-256 81d93733e869e17166e177f88aba9224729c16265ab33d7d6ea58edb9085c35e |
| H2     | CURRENT_PROJECT_STATE_LATEST.json, Eingangsstand dieses Arbeitsblocks                 | strukturierte Werte, Klassifikationen und Freeze-Regeln                                     | Eingangs-SHA-256 50224e7714752eda017406cd6465de09b4f0e1a68e87e4613a2b511cfbd91da3 |
| A1     | Apeiron_Anlage_A_Falsifizierbare_Vorhersagen_v1.0_2026-08-30.pdf                      | Abgrenzung und Prospektivstatus AP1-AP3                                                     | SHA-256 145ed65884c63d65c0e6fd042266cb01e4d2babcd370ac43745695ae62c532            |
| S1     | APEIRON_CANONICAL_MODEL_SPECIFICATION_LATEST.md                                       | operationale homogene Gleichungen, Einheiten, Parameter, Freiheitsgrade, diskrete Abbildung | Version 1.0; aktiver Quellpfad hashgebunden                                       |
| G1     | APEIRON_V7_13_GATE_SPECIFICATION_LATEST.json                                          | exakte v7.13-Schwellen, Operatoren, beobachtete Werte und Klassifikationsregeln             | Version 1.0; auf Protokoll, Gate-Register und Resultat gehasht                    |
| M1     | APEIRON_REPRODUCIBILITY_MANIFEST_LATEST.json                                          | SHA-256-Verzeichnis der Resultate, Zustände, Protokolle und aktiven Quellen                 | Version 1.0                                                                       |
| V1     | verify_apeiron_publication_package.py                                                 | read-only Hash-, Identitäts-, Form-, Gate- und Crossing-Prüfung                             | PASS; keine Solverimporte und keine Auswertung der physikalischen Abbildung       |
| U1     | STAGE00_HARD_PASS_RESULT_v7_13.json                                                   | terminale Werte, Klassifikation, Evaluationsanzahl                                          | SHA-256 030f83d808d00cafb2e9a9d80385ce9dde7b7b6193ebe46f87000a748411c5f           |
| U2     | STAGE00_HARD_PASS_SOLUTION_v7_13.npz                                                  | gespeicherte Arrays t, y, x, tau                                                            | SHA-256 72c01e17d8416d84264fa8ab8f33980f8ffd770203ace2f8078b86a42d4c3b53          |
| U3     | RECOVERY_GATE_REGISTER_v7_13_STAGE00.json                                             | v7.13-Gates und HARD_PASS                                                                   | SHA-256 1cd8d5008f0a6d599dad8c81e36fb32ca86a81dec34576e8935269f1781267245         |
| U4     | RECOVERY_PROTOCOL_v7_13.json                                                          | strikte Schwellen, Dimension, Solverbudget, Protokoll-tau                                   | SHA-256 25697b2dc6e15cfac4ca1393ea5521b31ca120f54710308c370057da98137129          |
| U5     | CROSSING_RESOLUTION_RESULT_v7_13.json                                                 | Float64-Nachbarschaft und Abbruchregel                                                      | SHA-256 87f899702f5d46abb2cf26affad67946a6fd8140b67402b2f23bf984afba098f          |
| U6     | v6.74 NONPASS-Resultat, -Solution und Gate-Register                                   | unveränderlicher Gegenendpunkt und seine eigene Klassifikation                              | Hashes in M1                                                                      |
| U7     | CURRENT_STATE_LATEST.npz, MASTER_RECOVERY_STATE_LATEST.json, CURRENT_META_LATEST.json | terminale Checkpointidentität, Arrays und Evaluation-Meta                                   | Hashes in M1; nur gelesen                                                         |
| U8     | aktive Laufzeitquellen aus dem Latest-Runtime-Capsule                                 | exakte operationale Implementierung                                                         | Einzelhashes in S1 und M1                                                         |

Evidenzregel: Resultatwerte stammen aus U1/U3/U5 beziehungsweise U6. Schwellen stammen aus U3/U4/G1 und niemals aus einer Schätzung anhand der Resultatwerte. Gleichungen stammen nur aus dem aktiven, in U8 identifizierten Ausführungspfad. S1 macht diesen Pfad publikationslesbar, erhebt ihn aber nicht nachträglich zu einer fundamentalen Wirkung.

### 3. Klassifikationsvokabular

| Klasse                                           | Bedeutung                                                                        |
|--------------------------------------------------|----------------------------------------------------------------------------------|
| Modellpostulat                                   | gesetzte physikalische oder ontologische Ausgangsannahme                         |
| mathematisch innerhalb des Modells hergeleitet   | folgt aus den angegebenen operationalen Gleichungen oder aus IEEE-754-Arithmetik |
| numerisch demonstriert                           | im eingefrorenen diskreten Lauf berechnet und gespeichert                        |
| durch Gates oder Klassifikation bestätigt        | erfüllt die vorregistrierte numerische Entscheidungsregel                        |
| wissenschaftliche Interpretation                 | vorsichtige Bedeutungsaussage jenseits des Zahlenwerts                           |
| offene Hypothese                                 | noch nicht hergeleitete oder gemessene physikalische Aussage                     |
| zukünftige messbare Vorhersage                   | prospektiver Observable- oder Nulltest aus Anlage A                              |
| unzulässige oder noch nicht gedeckte Überaussage | wird durch den Evidenzsatz nicht getragen                                        |

### 4. Zentrale Claims

#### 4.1 Modell, Gleichungen und diskrete Definition

| ID    | Aussage                                                                                                                  | Klasse                                       | Exakter Nachweis                 | Maximal zulässige Publikationsformulierung                                                                                                                     | Unzulässige stärkere Formulierung                                       |
|-------|--------------------------------------------------------------------------------------------------------------------------|----------------------------------------------|----------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------|
| C-001 | Untersucht wird ein eingefrorenes homogenes Apeiron/AME-1-FRW-Modell.                                                    | Modellpostulat / dokumentierte Struktur      | S1 Abs. 1-3; U8                  | "We study a frozen homogeneous FRW numerical model, operationally denoted Apeiron/AME-1."                                                                      | "Apeiron is established as the fundamental substrate of nature."        |
| C-002 | Natürliche Einheiten, $M_{pl} = 1$ , $\tau = H_{star} t$ , flaches FRW und $H > 0$ definieren den operationalen Rahmen.  | Modellpostulat                               | S1 Abs. 2                        | "The registered implementation uses the units, time coordinate and expanding flat-FRW branch stated in the supplement."                                        | "These conventions are uniquely required by nature."                    |
| C-003 | Die aktive diskrete Zustandsvariable umfasst sechs Trajektorien; der Vollcontainer umfasst acht.                         | Modellpostulat / dokumentierte Struktur      | S1 Abs. 3; U2; U7                | "The fixed-point vector stores six scaled trajectory columns; the released solution container stores eight columns."                                           | "The theory has exactly six fundamental degrees of freedom."            |
| C-004 | Homogenes $\chi$ wird nicht iteriert; der $\chi$ -Sektor tritt über $\rho_q$ , $p_q$ und $\langle \chi^2 \rangle_q$ ein. | Modellpostulat / operational definiert       | S1 Abs. 3 und 6; U8              | "The registered homogeneous map couples the portal sector through renormalized mode expectation values rather than an iterated homogeneous $\chi$ coordinate." | "All possible $\chi$ dynamics have been solved."                        |
| C-005 | Die Druckfunktion P, ihre Ableitungen, der Portalterm und die homogenen Gleichungen sind operational angegeben.          | mathematisch innerhalb des Modells definiert | S1 Abs. 5-7; U8-Hashes           | "The supplement provides the defining homogeneous pressure, derivatives, portal terms and evolution map used by v7.13."                                        | "A unique fundamental covariant action has been derived."               |
| C-006 | Die positive Friedmann-Wurzel schließt H in der Bildabbildung; Raychaudhuri bleibt ein unabhängiger Diagnoseweg.         | mathematisch innerhalb des Modells definiert | S1 Abs. 7 und 9; rb23-Hash in U8 | "The image map imposes the positive Friedmann branch and audits the Raychaudhuri relation independently."                                                      | "General covariance is thereby proven."                                 |
| C-007 | Das diskrete Gitter besitzt 15361 Knoten und der Float64-Vektor 92166 Komponenten.                                       | Modellpostulat / numerische Methode          | S1 Abs. 3 und 9; U2; U4          | "The frozen discretization contains 15361 nodes and a 92166-component Float64 fixed-point vector."                                                             | "The continuum solution is established."                                |
| C-008 | Die aktive Laufzeitquelle ist durch Einzelhashes gebunden.                                                               | Dokumentationsnachweis                       | S1 Abs. 10; M1                   | "The operational definition is tied to the hash-identified active runtime sources."                                                                            | "The implementation is independently certified as bug-free."            |
| C-009 | Eine eindeutige fundamentale Wirkung ist nicht Bestandteil des Belegsatzes.                                              | offene wissenschaftliche Lücke               | S1 Abs. 1 und 11                 | "The present paper defines the homogeneous model operationally and does not claim a unique fundamental covariant action."                                      | Jede Behauptung, eine fundamentale Wirkung sei bewiesen oder eindeutig. |

## 4.2 v7.13-Methode, Gates und Ergebnis

| ID    | Aussage                                                                                                                                                         | Klasse                                             | Exakter Nachweis                                                                                                                                          | Maximal zulässige Publikationsformulierung                                                                                                                        | Unzulässige stärkere Formulierung                                          |
|-------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------|
| C-010 | v7.13 Stage 0 verwendet binär $\tau = 0.47878124999999994$ und den dokumentierten exakten Protokollwert.                                                        | numerisch demonstriert                             | U1, U3, U4, G1                                                                                                                                            | "The terminal Stage-0 evaluation used the stated binary64 endpoint and exact protocol decimal."                                                                   | " $\tau$ is a measured constant of nature."                                |
| C-011 | v7.13 wurde einmal aus dem hashverifizierten v7.12-HARD-PASS initialisiert.                                                                                     | Dokumentationsnachweis                             | H1/H2; U4                                                                                                                                                 | "The persistent protocol records one initialization from the immutable v7.12 HARD-PASS state."                                                                    | "The entire history was independently rerun."                              |
| C-012 | Der geerbte Zustand erfüllte bereits das Fixed-Point-Gate; v7.13 führte null Newton-Schritte aus.                                                               | numerisch demonstriert / klassifiziert             | U1, U3, U7; G1                                                                                                                                            | "The inherited v7.13 state passed the fixed-point criterion before any Newton update; zero Newton steps were executed."                                           | "The solver converges without iteration for arbitrary states."             |
| C-013 | Fixed-Point und Friedmann betragen $4.6838977141305804e-11$ und $3.818888298257304e-12$ .                                                                       | numerisch demonstriert                             | U1, U3, G1                                                                                                                                                | "The recorded fixed-point and Friedmann diagnostics are the stated values."                                                                                       | "Both equations are exact."                                                |
| C-014 | Kontinuität, Raychaudhuri, Quantensource und Wronskian haben die gespeicherten Werte.                                                                           | numerisch demonstriert                             | U1, U3, G1                                                                                                                                                | "The recorded terminal diagnostics are $3.7214611922998273e-06$ , $1.4051164250399966e-05$ , $3.883856960984437e-08$ and $7.432742701266731e-09$ , respectively." | "Their smallness confirms physical reality."                               |
| C-015 | Die Positivitäts- und Hyperbolizitätsminima sind positiv und Endlichkeit ist wahr.                                                                              | numerisch demonstriert / durch Gates bestätigt     | G1: min $\rho = 2.0729288609194362e-14$ ; min $H = 8.312498343027667e-08$ ; min $P_X = 1.0523451240627972$ ; min kinetischer Nenner = $1.052350229025336$ | "The recorded positivity, hyperbolicity and finiteness gates pass at the terminal state."                                                                         | "Global stability and causality are proven."                               |
| C-016 | Die strikten Schwellen sind $FP < 5e-11$ , $Friedmann < 1e-10$ , $Kontinuität < 1e-5$ , $Raychaudhuri < 2e-5$ , $Quantensource < 1e-7$ und $Wronskian < 2e-8$ . | Modellpostulat / registrierte Klassifikationsregel | U3, U4, G1                                                                                                                                                | "The terminal classification uses the exact strict thresholds listed in the released gate specification."                                                         | Schwellen aus den beobachteten Werten herleiten oder nachträglich lockern. |
| C-017 | Weitere Gates verlangen $\rho > 0$ , $H > 0$ , $P_X > 0$ , kinetischen Nenner $> 0$ , Endlichkeit wahr und keinen Finalisierungsfehler.                         | registrierte Klassifikationsregel                  | U3, U4, G1                                                                                                                                                | "The remaining gates impose the listed positivity, hyperbolicity, finiteness and finalization conditions."                                                        | "Passing these local gates proves full theoretical consistency."           |
| C-018 | Alle v7.13-Gates bestanden; die Klassifikation lautet HARD_PASS.                                                                                                | durch Gates oder Klassifikation bestätigt          | U1, U3, G1                                                                                                                                                | "Under the frozen v7.13 protocol, Stage 0 satisfies every registered gate and is classified HARD_PASS."                                                           | "Apeiron is empirically confirmed."                                        |
| C-019 | Das registrierte Budget umfasst maximal 6 Newton-Schritte, GMRES restart 10, höchstens 16 Zyklen, rtol 0.05, JVP-Schritt $1e-5$ und 13 Halbierungs-Alpha's.     | Modellpostulat / reproduzierbare Methode           | U4, G1                                                                                                                                                    | "The released protocol records the stated nonlinear-solver budget, although v7.13 consumed no Newton update."                                                     | "These settings are universally optimal."                                  |
| C-020 | Die v7.13-Solution enthält $t$ , $y$ , $x$ und $\tau$ in den registrierten Formen und Float64.                                                                  | Dokumentationsnachweis                             | U2; V1 PASS                                                                                                                                               | "The released solution arrays have the registered keys, shapes and Float64 dtypes."                                                                               | "The stored trajectory was independently recomputed."                      |

### 4.3 Gegenendpunkt, Crossing und Reproduzierbarkeit

| ID    | Aussage                                                                                                                 | Klasse                                                       | Exakter Nachweis                               | Maximal zulässige Publikationsformulierung                                                                                         | Unzulässige stärkere Formulierung                                 |
|-------|-------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------|------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------|
| C-021 | v6.74 bei $\tau = 0.47878125$ ist NONPASS; Fixed Point und Friedmann verfehlten seine registrierten Gates.              | numerisch demonstriert / klassifiziert                       | U6; H1/H2                                      | "The immutable v6.74 endpoint is NONPASS because its fixed-point and Friedmann gates fail."                                        | "Nature is unstable above this value."                            |
| C-022 | Die v6.74-Toleranzen dürfen nicht als v7.13-Schwellen verwendet werden.                                                 | Klassifikationsregel                                         | G1; U3/U4 versus U6                            | "The historical v6.74 gate table is not substituted for the strict v7.13 table."                                                   | Gate-Tabellen vermischen.                                         |
| C-023 | v7.13-HARD-PASS und v6.74-NONPASS sind benachbarte Float64-Werte.                                                       | mathematisch innerhalb IEEE-754 / dokumentiert               | U5; V1 PASS                                    | "The two classified binary64 endpoints are adjacent representable values."                                                         | "The exact physical transition has been located."                 |
| C-024 | Der exakte Protokollmittelpunkt rundet auf den NONPASS-Binärwert; weitere Float64-Bisektion ist verboten.               | mathematisch innerhalb des Protokolls / Klassifikationsregel | U5; V1 PASS mit Decimal- und nextafter-Prüfung | "The exact protocol midpoint maps to the recorded NONPASS binary64 endpoint; the frozen Float64 schedule therefore terminates."    | "No intermediate real number exists."                             |
| C-025 | Der read-only Verifier bestätigt Hashes, Identitäten, Formen, gespeicherte Gatevergleiche und Crossing-Regeln.          | Dokumentationsnachweis                                       | M1; V1 PASS                                    | "A read-only verifier confirms package integrity and documentary consistency."                                                     | "The physical calculation was independently reproduced."          |
| C-026 | Im Publikationsaudit wurde weder der Solver noch die physikalische Abbildung ausgeführt.                                | wissenschaftliche Abgrenzung                                 | V1 Quelltext; Meta; Prozessprotokoll           | "The audit performed no solver rerun and recomputed no physical diagnostic."                                                       | "The v7.13 result has been independently numerically reproduced." |
| C-027 | Das Paket ist bis zur read-only Integritätsstufe reproduzierbar; unabhängige Implementierungsreproduktion bleibt offen. | wissenschaftliche Interpretation                             | README_REPRODUCIBILITY.md; M1; V1              | "The release supports file-level and documentary verification; independent implementation-level reproduction remains future work." | "Complete independent reproducibility has been achieved."         |

### 4.4 Physik, Empirie und Ontologie

| ID    | Aussage                                                                                      | Klasse                           | Exakter Nachweis                       | Maximal zulässige Publikationsformulierung                                                                   | Unzulässige stärkere Formulierung                                        |
|-------|----------------------------------------------------------------------------------------------|----------------------------------|----------------------------------------|--------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------|
| C-030 | Der HARD_PASS belegt technische Gate-Erfüllung für diesen diskreten Zustand.                 | wissenschaftliche Interpretation | C-010-C-020                            | "The HARD-PASS establishes compliance with the registered numerical criteria for the frozen discretization." | "The whole theory is correct."                                           |
| C-031 | Der HARD_PASS ist keine Kontinuumskonvergenz oder globale Stabilitätsaussage.                | Abgrenzung                       | S1 Abs. 9; keine entsprechende Evidenz | "No continuum-convergence or global-stability claim is made."                                                | "The continuum theory is stable."                                        |
| C-032 | Der HARD_PASS ist keine empirische Bestätigung.                                              | Abgrenzung                       | A1; keine Datenanalyse                 | "No observational comparison is reported; empirical support remains open."                                   | "Observations confirm Apeiron."                                          |
| C-033 | Der HARD_PASS ist keine ontologische Bestätigung eines Apeiron-Mediums.                      | Abgrenzung                       | S1 Abs. 1; A1                          | "The calculation does not establish an Apeiron ontology."                                                    | "The medium has been detected."                                          |
| C-034 | Physikalische Plausibilität ist von technischer Korrektheit zu trennen.                      | wissenschaftliche Interpretation | S1; Lückenbericht                      | "Internal numerical consistency is necessary but insufficient for physical plausibility."                    | "Numerical consistency makes the model physically true."                 |
| C-035 | Ein eindeutiges physikalisches Mapping von $\tau$ ist offen.                                 | offene Hypothese / Grenze        | A1 AP1                                 | "The physical mapping of $\tau$ is deferred to AP1."                                                         | " $\tau$ already equals redshift, time or scale factor in a unique way." |
| C-036 | Lineare Störungen und etablierte Beobachtungsgrenzen sind nicht im v7.13-Ergebnis enthalten. | offene wissenschaftliche Lücke   | A1; S1 Abs. 1                          | "Perturbations and observational consistency require separate follow-up analysis."                           | "v7.13 passes cosmological observations."                                |

## 4.5 Zukünftige falsifizierbare Vorhersagen

| ID    | Aussage                                                                                                     | Klasse                                      | Exakter Nachweis      | Maximal zulässige Publikationsformulierung                                                                    | Unzulässige stärkere Formulierung                     |
|-------|-------------------------------------------------------------------------------------------------------------|---------------------------------------------|-----------------------|---------------------------------------------------------------------------------------------------------------|-------------------------------------------------------|
| C-040 | AP1 soll Expansion, Wachstum und Lensing mit einem gemeinsamen Parametersatz ableiten.                      | zukünftige messbare Vorhersage              | A1 S. 3-4             | "AP1 prospectively targets a jointly parameterized expansion-growth-lensing observable vector."               | "The curves are already predicted."                   |
| C-041 | AP1 setzt eindeutiges $\tau$ -Mapping, geschlossene Störungen und Stabilitätsgates vor Datenkontakt voraus. | zukünftiges methodisches Gate               | A1 S. 4 und 9         | "AP1 proceeds only after the physical map, perturbations and preregistered stability checks are fixed."       | "These prerequisites are already fulfilled."          |
| C-042 | AP2 definiert einen zukünftigen Filament-Residual test mit Materierekonstruktion und Nulltests.             | offene Hypothese / zukünftige Vorhersage    | A1 S. 5, 7-8          | "AP2 will test a preregistered residual filament-lensing profile after matter reconstruction and null tests." | "Filaments already show Apeiron gravity."             |
| C-043 | AP3 behandelt $c_{GW} = c$ als Überlebensbedingung und soll mögliche Propagationsobservablen ableiten.      | offene Hypothese / zukünftige Vorhersage    | A1 S. 6               | "AP3 is a prospective tensor-sector test constrained by the gravitational-wave speed condition."              | "Apeiron causes measured GW damping or polarization." |
| C-044 | AP1-AP3 müssen einen gemeinsamen eingefrorenen Parameterkern verwenden.                                     | Modellpostulat für zukünftige Falsifikation | A1 S. 1, 3, 7-8       | "The program forbids independent channel-by-channel retuning."                                                | "Three separate fits jointly confirm Apeiron."        |
| C-045 | Anlage A ist kein empirischer Nachweis und kein Teil des HARD_PASS.                                         | Abgrenzung                                  | A1 S. 1-2 und 9       | "Appendix A is a prospective falsification roadmap, separate from v7.13."                                     | "AP1-AP3 were validated by v7.13."                    |
| C-046 | Es existieren keine freigegebenen Vorhersagekurven, Messwerte oder empirischen PASS-Ergebnisse.             | Abgrenzung                                  | A1; Publikationspaket | "No observable template, fitted curve or empirical PASS is claimed."                                          | Erfundene Kurven, Signifikanzen oder Best-fit-Werte.  |

## 4.6 Publikationsstatus und ausgeschlossene Motive

| ID    | Aussage                                                                                                                                  | Klasse                  | Exakter Nachweis                               | Maximal zulässige Publikationsformulierung                                                                                | Unzulässige stärkere Formulierung                               |
|-------|------------------------------------------------------------------------------------------------------------------------------------------|-------------------------|------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------|
| C-050 | Der wissenschaftlich-technische Kern kann nun als kontrollierter Preprintentwurf paketiert werden.                                       | Dokumentierter Status   | S1, G1, M1, V1 PASS; Manuskript; Lückenbericht | "The controlled technical core is documented for preprint packaging, subject to editorial and administrative completion." | "The work is peer-reviewed, accepted or empirically validated." |
| C-051 | Eine Journaleinreichung benötigt weiterhin Autorenangaben, Deklarationen, Venue-Format und finale Archiv-/Lizenzangaben.                 | redaktionelle Grenze    | Manuskriptplatzhalter; Publikationsmeta        | "Venue-specific submission preparation remains outstanding."                                                              | "The journal submission package is complete."                   |
| C-052 | Genesis, ewiger Kreislauf, reale Apeiron-Filamente und Schwarze Löcher als Apeiron-Fenster sind im aktuellen Ergebnisscope nicht belegt. | unzulässige Überaussage | fehlen in H1/H2/A1/S1/G1                       | "These motifs are not results of the present numerical-foundations paper."                                                | "The calculation proves any of these motifs."                   |

## 5. Fünf strikt getrennte Aussageebenen

1. Technische Korrektheit des Rechenteils: Die eingefrorenen Resultat-, Zustands-, Protokoll- und Gate-Dateien sind hashverifiziert und dokumentarisch konsistent. V1 ist keine neue numerische Reproduktion.
2. Konsistenz des dokumentierten Modells: v7.13 erfüllt die exakten registrierten Gates des angegebenen homogenen diskreten Modells.
3. Physikalische Plausibilität: bleibt teilweise offen; insbesondere fehlen Kontinuumsnachweis, Störungen, globale Stabilität und vollständige externe Konsistenztests.
4. Empirische Bestätigung: nicht vorhanden; AP1-AP3 sind prospektiv.
5. Ontologische Interpretation: ein Apeiron-Medium bleibt Modellpostulat beziehungsweise offene Hypothese.

## 6. Kontrollierte Wortwahl

| Ausdruck     | Zulässig                                                                        | Unzulässig                                          |
|--------------|---------------------------------------------------------------------------------|-----------------------------------------------------|
| Beweis       | elementare Float64-Nachbarschaft, ausdrücklich auf Repräsentation begrenzt      | physikalische Existenz oder Wahrheit von Apeiron    |
| Bestätigung  | Bestätigung der gespeicherten Gate-Erfüllung oder Dateiintegrität               | Bestätigung der Theorie oder empirische Bestätigung |
| Nachweis     | Dokumentations- oder Integritätsnachweis mit genauer Quelle                     | Nachweis eines Mediums oder neuer Gravitation       |
| stabil       | nur bestandene lokale Hyperbolizitäts-/Positivitätsgates am angegebenen Zustand | globale, nichtlineare oder kosmologische Stabilität |
| Grenze       | Float64-Klassifikationsklammer unter dem gefrorenen Protokoll                   | exakte physikalische Phasengrenze                   |
| reproduziert | nur bei echter unabhängiger Neuberechnung                                       | für den read-only Dokumentationsprüfer              |

## 7. Claims-Freeze

Die Claims C-001 bis C-052 sind der aktualisierte interne Freeze. Externe Literatur darf Motivation, methodischen Kontext und Beobachtungsgrenzen ergänzen, aber weder die eingefrorene interne Modellabbildung ändern noch fehlende Physik ersetzen. Stärkere Aussagen als die Spalte "maximal zulässige Publikationsformulierung" sind ausgeschlossen.

## Part II - Venue-neutral master manuscript

English scientific draft with numerical results, limitations, and future falsification program

# Apeiron/AME-1: Terminal Numerical Classification of a Frozen Homogeneous Model and a Prospective Falsification Program

Venue-neutral master manuscript - controlled technical draft Author(s): [AUTHORSHIP TO BE PROVIDED] Affiliation(s): [AFFILIATION TO BE PROVIDED] Corresponding author: [TO BE PROVIDED] Status: technical core documented for preprint packaging; venue-specific and administrative completion outstanding Numerical reference: terminal v7.13 Stage-0 HARD-PASS; Float64 crossing schedule complete and frozen

## 1. Title and cautious abstract

### Abstract

We report the terminal numerical classification of a frozen homogeneous Apeiron/AME-1 model and separate this result from physical, empirical and ontological claims. The model is defined operationally on a spatially flat expanding FRW background by a noncanonical pressure function, a portal-coupled renormalized mode source and a discrete fixed-point map on 15361 time nodes. At the binary64 endpoint  $\tau=0.478781249999999994$ , corresponding to the exact protocol decimal 0.478781249999999994315658113919198513031005859375, the inherited v7.13 state already satisfied the fixed-point criterion and required no Newton or GMRES update. The recorded fixed-point, Friedmann, continuity, Raychaudhuri, quantum-source and Wronskian diagnostics are  $4.6838977141305804 \times 10^{-11}$ ,  $3.818888298257304 \times 10^{-12}$ ,  $3.7214611922998273 \times 10^{-6}$ ,  $1.4051164250399966 \times 10^{-5}$ ,  $3.883856960984437 \times 10^{-8}$  and  $7.432742701266731 \times 10^{-9}$ , respectively. All preregistered v7.13 gates passed and no finalization failure was recorded, yielding a HARD-PASS under the frozen protocol. The adjacent binary64 endpoint  $\tau=0.47878125$  is an immutable v6.74 NONPASS because its fixed-point and Friedmann gates failed. The classified endpoints are adjacent representable values; the exact protocol midpoint rounds to the NONPASS endpoint, terminating the frozen Float64 schedule. The release includes the operational equations, exact gate table, hash manifest, immutable artifacts and a read-only integrity verifier. This verifier does not rerun the solver or recompute physical diagnostics. The result therefore establishes compliance with the stated numerical criteria for this discretization, not continuum convergence, empirical confirmation or an Apeiron ontology. AP1-AP3 are presented only as a prospective falsification program; no observable curve, data fit or empirical preference is claimed.

Keywords: numerical cosmology; fixed-point residual; gate classification; binary64 boundary; reproducibility; falsifiability

## 2. Motivation and problem statement

Foundational model programs face distinct burdens of evidence. First, their internal equations and numerical decisions must be explicit enough to audit. Second, their computations must satisfy declared criteria without retrospective changes. Third, their physical interpretation must be converted into observables and compared with data. Passing one burden does not discharge the others.

The present work addresses the first two burdens for one frozen homogeneous Apeiron/AME-1 calculation. It asks:

1. What model and discrete map were actually evaluated?
2. What exact rules produced the terminal PASS/NONPASS classifications?

3. What does the terminal result establish, and what remains open?

4. How can later observable tests be preregistered without changing the completed numerical line?

The v7.13 result and its adjacent v6.74 counter-endpoint are treated as immutable. No solver rerun, gate change, parameter adjustment or new physical assumption is introduced in preparing this manuscript.

## 3. Definition and delimitation of the Apeiron model

### 3.1 Operational definition

The paper uses “Apeiron/AME-1” as the name of a frozen homogeneous numerical model. Its authoritative publication definition is operational: the variables, parameters, pressure function, portal coupling, quantum-source prescription, background equations, initial data, discretization and active source hashes are stated in APEIRON\_CANONICAL\_MODEL\_SPECIFICATION\_LATEST.md.

The background is spatially flat FRW with scale factor  $a$ , e-fold variable  $N=\ln a$ , Hubble rate  $H>0$ , natural units  $c=\hbar=1$  and reduced Planck mass  $M_{\text{pl}}=1$ . The numerical time coordinate is

$$\tau = H_{\text{star}} \int_t^{\tau} \frac{d\tau}{H(\tau)} = \frac{1}{H_{\text{star}}} \ln \left( \frac{H(\tau)}{H_{\text{star}}} \right).$$

### 3.2 Scope

The registered calculation is homogeneous and background-level. It does not contain:

- a unique fundamental covariant action;
- a closed scalar, vector or tensor perturbation theory;
- a continuum-limit demonstration;
- a global or nonlinear stability theorem;
- an observational likelihood analysis;
- an ontological test of an Apeiron medium.

The lack of a unique action-level completion is not concealed. It limits the article to the exact operational discrete model that was computed.

### 3.3 Meaning of the control parameter

$\tau$  is the registered numerical time/control endpoint of the frozen calculation. A unique observational or cosmological mapping beyond  $\tau = H_{\text{star}} t$ , including any direct mapping to redshift, remains an AP1 task. The terminal Float64 bracket must therefore not be described as a measured physical constant or exact physical phase boundary.

## 4. Frozen assumptions, degrees of freedom and equations

### 4.1 Stored state and degrees of freedom

The full trajectory container is

$$\mathbf{y} = (\sigma, \dot{\sigma}, \theta, \dot{\theta}, \chi, \dot{\chi}, H, N).$$

The iterated state uses six columns,

$$\mathbf{u} = (\sigma, \dot{\sigma}, \theta, \dot{\theta}, H, N),$$

while the homogeneous  $\chi$  bookkeeping coordinate is fixed to zero. The portal sector enters through renormalized mode expectation values  $\rho_q$ ,  $p_q$  and  $\langle \chi^2 \rangle_q$ . This six-column numerical state is not claimed to be a count of fundamental degrees of freedom in an unknown covariant completion.

The fixed-point vector is the flattened scaled state

$$\mathbf{x} = \text{vec} \left( \frac{\sigma}{10^{-2}}, \frac{\dot{\sigma}}{10^{-8}}, \theta, \frac{\dot{\theta}}{10^{-8}}, \frac{H}{10^{-6}}, \frac{N}{10^{-1}} \right),$$

with 15361 nodes, 92166 Float64 components and a full stored solution array of shape  $15361 \times 8$ .

### 4.2 Homogeneous pressure

Define

$$X = \frac{1}{2} \dot{\theta}^2, \quad z = \frac{\sigma}{f_{\sigma}}, \quad b = b_{\text{star}} + b_{\text{slope}} \frac{\theta}{M_{\text{pl}} - (5X)/(\Lambda b^4)},$$

$$F(z,b)=\frac{14z^4-12z^2+bz}{\dots}$$

The registered pressure is

$$P(X,\sigma,\theta) = X + (5)/(3\Lambda^4) \sqrt{(z-(2)/(\sqrt{3}))^2 X^2 - E_c F(z,b) - V_s(\theta)},$$

where  $V_s(\theta) = \sum_{i=0}^4 c_i \theta^i$  and the five frozen coefficients are given in the canonical specification. The executable derivatives  $P_X$ ,  $P_{XX}$ ,  $P_\sigma$ ,  $P_\theta$  and  $P_{X\sigma}$  are stated there in full.

The AME stress is

$$\rho_{AME} = \frac{12\dot{\sigma}^2 + 2XP_X - P}{\dots}, \quad p_{AME} = \frac{12\dot{\sigma}^2 + P}{\dots}$$

### 4.3 Portal and quantum source

The field-dependent portal mass is

$$m_{\chi^2} = m_{\chi,0}^2 + 2\Lambda(v+\sigma)^2 \cos\left(\frac{2\theta}{f_{\text{phase}}}\right).$$

The quantum routine uses four Pauli-Villars sectors with coefficients (1,-3,3,-1), regulator indices (0,1,2,3), 128 resolved momentum nodes on the initial physical support  $0 \leq k \leq 0.6\Lambda$ , an analytic order-0 tail and auxiliary adiabatic curvature orders 2 and 4. Mode functions are advanced by a three-substep Yoshida composition of an implicit-midpoint update.

The normalized quantum-source diagnostic represents

$$\text{dot}\rho_q + 3H(\rho_q + p_q) - \frac{12}{\dots} m_{\chi^2}(\chi^2)_q = 0.$$

### 4.4 Registered background map

With  $\rho_{\text{tot}} = \rho_{AME} + \rho_q$  and  $p_{\text{tot}} = p_{AME} + p_q$ , the image map integrates

$$\ddot{\sigma} = -3H\dot{\sigma} + P_\sigma - \frac{12}{\dots} \partial_\sigma m_{\chi^2}(\chi^2)_q,$$

$$\ddot{\theta} = \frac{P_\theta - \frac{12}{\dots} \partial_\theta m_{\chi^2}(\chi^2)_q - 3HP_X \dot{\theta} - P_X \dot{\sigma} \dot{\theta}}{P_X + 2XP_{XX}},$$

$$H = \sqrt{\frac{\rho_{\text{tot}}}{3M_{\text{pl}}^2}}, \quad \text{quad } \dot{N} = H.$$

The Raychaudhuri relation

$$\dot{H} = -\frac{\rho_{\text{tot}} + p_{\text{tot}}}{2M_{\text{pl}}^2}$$

is retained as an independent diagnostic. Hyperbolicity gates require  $P_X > 0$  and  $P_X + 2XP_{XX} > 0$ .

### 4.5 Fixed-point definition

For the hash-identified image map  $\mathbf{G}$ ,

$$\mathbf{R}(\mathbf{x}; \tau) = \mathbf{x} - \mathbf{G}(\mathbf{x}; \tau), \quad \text{quad } \delta_{FP} = \|\mathbf{R}\|_\infty.$$

All parameters, source files, gates, tolerances, discretization and solver budgets were frozen before the terminal classification.

## 5. Numerical method and reproducibility

### 5.1 Discretization and nonlinear budget

The grid spacing is  $\Delta\tau = \tau_{\text{end}}/15360$ . The registered finite-difference step for Jacobian-vector products is  $10^{-5}$ . The allowed nonlinear budget was:

- at most 6 Newton steps;
- GMRES restart 10;
- at most 16 GMRES cycles per Newton step;
- GMRES relative tolerance 0.05 and absolute tolerance 0;
- line-search factors  $2^{-j}$ ,  $j=0,\dots,12$ .

These values describe the frozen allowance. The terminal v7.13 evaluation consumed no Newton update because the inherited state already passed the fixed-point gate.

### 5.2 Persistence and immutability

The v7.13 result JSON, solution NPZ, gate register, protocol, crossing decision, terminal checkpoint state and active runtime sources are individually hashed in APEIRON\_REPRODUCIBILITY\_MANIFEST\_LATEST.json. The adjacent v6.74 result, solution and gate register are also included. The v6.74 gate table is preserved for its own classification and is not substituted for the strict v7.13 table.

### 5.3 Read-only verification

The accompanying verifier:

- 1. checks every registered SHA-256 digest;
- 2. checks cross-document identities and terminal metadata;
- 3. checks NPZ keys, shapes and Float64 dtypes;
- 4. compares the stored diagnostics with the immutable gate table;
- 5. checks binary64 endpoint adjacency and exact-protocol midpoint rounding.

It imports no solver module, evaluates no physical map and modifies no file. Its passing terminal message is APEIRON\_PUBLICATION\_PACKAGE\_VERIFY\_PASS. This is package-integrity verification, not independent numerical reproduction.

### 5.4 Reproducibility levels

| Level | Meaning                                                             | Status        |
|-------|---------------------------------------------------------------------|---------------|
| V0    | narrative and filenames                                             | passed        |
| V1    | narrative and structured handoff agree                              | passed        |
| V2    | immutable artifacts resolved and hashes verified                    | passed        |
| V2.5  | stored gates, array forms and crossing identities checked read-only | passed        |
| V3    | physical diagnostics independently recomputed from the stored state | not performed |
| V4    | independent implementation reproduces the classification            | open          |
| V5    | observable templates preregistered and tested                       | not begun     |

## 6. Gates, tolerances and classification rules

### 6.1 Exact v7.13 gate table

| Gate                      | Operator | Threshold             | Recorded value                       | Result |
|---------------------------|----------|-----------------------|--------------------------------------|--------|
| fixed-point infinity norm | <        | $5.0 \times 10^{-11}$ | $4.6838977141305804 \times 10^{-11}$ | pass   |
| Friedmann constraint      | <        | $1.0 \times 10^{-10}$ | $3.818888298257304 \times 10^{-12}$  | pass   |
| continuity residual       | <        | $1.0 \times 10^{-5}$  | $3.7214611922998273 \times 10^{-6}$  | pass   |
| Raychaudhuri residual     | <        | $2.0 \times 10^{-5}$  | $1.4051164250399966 \times 10^{-5}$  | pass   |
| quantum-source identity   | <        | $1.0 \times 10^{-7}$  | $3.883856960984437 \times 10^{-8}$   | pass   |
| Wronskian diagnostic      | <        | $2.0 \times 10^{-8}$  | $7.432742701266731 \times 10^{-9}$   | pass   |
| minimum total density     | >        | 0                     | $2.0729288609194362 \times 10^{-14}$ | pass   |
| minimum H                 | >        | 0                     | $8.312498343027667 \times 10^{-8}$   | pass   |
| minimum P_X               | >        | 0                     | 1.0523451240627972                   | pass   |
| minimum P_X+2 XP_XX       | >        | 0                     | 1.052350229025336                    | pass   |
| finite                    | is       | true                  | true                                 | pass   |
| finalization failure      | is       | null                  | null                                 | pass   |

### 6.2 Classification logic

HARD\_PASS requires every listed numerical gate to pass and the finalization-failure field to be null. PASS/NONPASS is a deterministic protocol classification. It is not a statistical p-value, likelihood statement, model-selection score or empirical verdict.

## 7. Results of the terminal v7.13 calculation

### 7.1 v7.13 endpoint

The terminal exact protocol value is

```
τ_ HP^ exact =0.47878124999999994315658113919198513031005859375,
```

stored as binary64

```
τ_ HP^64=0.47878124999999994.
```

The terminal record reports one physical-map evaluation, zero Newton steps, no iteration log, no finalization failure and HARD\_PASS. The exact diagnostic values and thresholds are listed in Section 6.

### 7.2 Immutable v6.74 counter-endpoint

The adjacent endpoint

```
τ_ NP^64=0.47878125
```

is classified NONPASS in the immutable v6.74 record. Its fixed-point diagnostic  $1.8866305739884126 \times 10^{-10}$  and Friedmann diagnostic  $1.7440413453847122 \times 10^{-10}$  failed the gates registered for that result; its remaining documented gates passed. The counter-endpoint is used only for the frozen crossing classification.

7.3 Float64 crossing resolution

| Quantity                       | Value                                                  |
|--------------------------------|--------------------------------------------------------|
| exact protocol bracket width   | $5.684341886080801486968994140625 \times 10^{-17}$     |
| binary64 bracket width         | $5.551115123125783 \times 10^{-17}$                    |
| next exact protocol midpoint   | 0.478781249999999971578290569595992565155029296875     |
| midpoint converted to binary64 | 0.47878125, the NONPASS endpoint                       |
| endpoint relation              | adjacent representable binary64 values                 |
| frozen decision                | schedule complete; further Float64 bisection forbidden |

The bracket is a representation- and protocol-dependent classification result. It is not an exact boundary in the real numbers or a measured physical uncertainty.

8. Physical interpretation

The result establishes a narrow technical fact: the stored v7.13 state meets the frozen numerical acceptance criteria, while the adjacent stored v6.74 endpoint is NONPASS. This closes the registered Float64 continuation schedule without reopening the solver.

The result does not demonstrate that the operational equations are unique, fundamental or empirically adequate. Passing positivity and hyperbolicity gates at the terminal trajectory does not prove global stability. Small residuals do not provide observational evidence. The ontology of an Apeiron medium remains a hypothesis outside the reach of the present calculation.

Physical plausibility requires separate work: action-level interpretation or another principled completion, perturbation dynamics, regulator and scheme analyses beyond the registered discrete scope, continuum/refinement evidence, comparison with established constraints and ultimately preregistered data tests.

9. Limits and unanswered questions

The principal open questions are:

1. Does the operational homogeneous model admit a defensible and sufficiently unique covariant completion?
2. Do the results persist under controlled grid and method refinement?
3. What are the linear scalar, vector and tensor perturbation equations?
4. Are the relevant sectors stable beyond the terminal background trajectory?
5. How is  $\tau$  mapped uniquely to observable cosmological variables?
6. Does one common parameter set satisfy expansion, growth, lensing, local and gravitational-wave constraints?
7. Can an independent implementation reproduce the terminal classification?

Items 1-7 constrain interpretation and later claims. They do not alter the already completed v7.13 classification. AP1-AP3 are not prerequisites for reporting this narrowly scoped numerical result.

10. Falsifiable predictions and future work

Appendix A defines a prospective program, not completed evidence.

10.1 AP1 - joint expansion, growth and lensing

AP1 is intended to derive  $H(z)$ ,  $w_{\text{ap}}(z)$ ,  $f\sigma_8(z)$ ,  $\mu(k,z)$ ,  $\eta(k,z)$  and  $\Sigma(k,z)$  from one frozen parameter core. Before data contact it requires a unique physical  $\tau$  mapping, closed perturbation equations, stability gates, fixed grids, priors, masks, likelihoods and versioned output templates. No such curves are reported here.

10.2 AP2 - residual filament gravity

AP2 prospectively tests a residual lensing profile after reconstruction of galaxies, gas and the declared comparison-model matter distribution:

$$\Delta\kappa_{\text{ap}} = F(r_{\perp}, z, d_{\text{node}}, \{ \text{curvature} | \theta_{\text{ap}} \}).$$

It must reuse the AP1 parameter core and pass prespecified void and rotated-axis null tests. No filament signal is claimed in this paper.

### 10.3 AP3 - gravitational-wave propagation

AP3 treats  $c_{\text{GW}}=c$  as a survival condition and prospectively derives amplitude, polarization or line-of-sight observables from a closed tensor sector. No modified-propagation detection is claimed.

### 10.4 Cross-channel decision rule

AP1-AP3 must use one preregistered parameter core. Channel-by-channel retuning is forbidden. A conflict with any hard gate produces NONPASS for the affected hypothesis rather than retrospective adjustment of v7.13.

## 11. Conclusion

The frozen Apeiron/AME-1 v7.13 Stage-0 state at binary64  $\tau=0.47878124999999994$  satisfies every exact registered gate and is classified HARD\_PASS. The adjacent binary64 endpoint  $\tau=0.47878125$  is an immutable v6.74 NONPASS because its fixed-point and Friedmann gates fail. The exact protocol midpoint converts to the NONPASS binary64 endpoint, so the registered Float64 crossing schedule is complete.

The publication package now states the operational homogeneous model, exact v7.13 thresholds, artifact hashes and a read-only verification path. These additions close the former documentary blockers without recomputing the physics. They do not establish continuum convergence, empirical confirmation or an Apeiron ontology. The technical core is suitable for controlled preprint packaging after editorial and administrative completion; venue-specific journal submission preparation remains outstanding. AP1-AP3 remain separate follow-up work.

## 12. Methods and reproducibility supplement

### 12.1 Controlled file manifest

| File                                                        | Role                                                         |
|-------------------------------------------------------------|--------------------------------------------------------------|
| APEIRON_CANONICAL_MODEL_SPECIFICATION_LATEST.md             | operational model, equations, units, state and source hashes |
| APEIRON_V7_13_GATE_SPECIFICATION_LATEST.json                | exact thresholds, operators, values and classification       |
| APEIRON_REPRODUCIBILITY_MANIFEST_LATEST.json                | SHA-256 manifest                                             |
| README_REPRODUCIBILITY.md                                   | verification scope and instructions                          |
| verify_apeiron_publication_package.py                       | read-only verifier                                           |
| TECHNICAL_SOURCES/STAGE00_HARD_PASS_RESULT_v7_13.json       | immutable terminal result                                    |
| TECHNICAL_SOURCES/STAGE00_HARD_PASS_SOLUTION_v7_13.npz      | immutable terminal arrays                                    |
| TECHNICAL_SOURCES/RECOVERY_GATE_REGISTER_v7_13_STAGE00.json | immutable terminal gate register                             |
| TECHNICAL_SOURCES/RECOVERY_PROTOCOL_v7_13.json              | immutable protocol                                           |
| TECHNICAL_SOURCES/CROSSING_RESOLUTION_RESULT_v7_13.json     | immutable crossing decision                                  |
| TECHNICAL_SOURCES/STAGE00_NONPASS_RESULT_v6_74.json         | immutable adjacent NONPASS result                            |
| TECHNICAL_SOURCES/STAGE00_NONPASS_SOLUTION_v6_74.npz        | immutable adjacent NONPASS arrays                            |
| TECHNICAL_SOURCES/RECOVERY_GATE_REGISTER_v6_74_STAGE00.json | immutable adjacent NONPASS register                          |
| TECHNICAL_SOURCES/STATE_SNAPSHOT                            | terminal read-only checkpoint snapshot                       |
| TECHNICAL_SOURCES/ACTIVE_RUNTIME                            | hash-frozen active source path                               |

All exact hashes are stored in the machine-readable manifest.

### 12.2 Verification command

From the package root:

```
python3 verify_apeiron_publication_package.py
```

Expected terminal line:  
APEIRON\_PUBLICATION\_PACKAGE\_VERIFY\_PASS

12.3 Data and code availability - controlled draft

The accompanying publication distribution contains the canonical operational specification, exact gate table, immutable result/state/protocol artifacts, active source path and read-only verifier. A permanent repository identifier, license and venue-specific availability wording remain to be assigned. No observational dataset was analyzed.

12.4 Statistical statement

No statistical fit, parameter estimation, hypothesis-test significance, Bayes factor, information criterion or observational model comparison is reported. PASS/NONPASS denotes only deterministic numerical gate classification.

12.5 Declarations

- Author contributions: [TO BE PROVIDED]
- Funding: [TO BE PROVIDED]
- Competing interests: [TO BE PROVIDED]
- Acknowledgments: [TO BE PROVIDED]
- Data/code license: [TO BE PROVIDED]
- AI-assisted drafting disclosure: [TO BE DECIDED ACCORDING TO VENUE POLICY]

13. Figure, table and data inventory

13.1 Figures

| Figure | Content                                                                                   | Status                                           |
|--------|-------------------------------------------------------------------------------------------|--------------------------------------------------|
| Fig. 1 | separation of numerical classification, physical interpretation and future empirical test | specified; artwork pending                       |
| Fig. 2 | adjacent v7.13 HARD_PASS and v6.74 NONPASS binary64 endpoints                             | data fully specified; artwork pending            |
| Fig. 3 | AP1 → AP2 → AP3 dependency and common parameter freeze                                    | concept specified in Appendix A; artwork pending |

13.2 Tables

| Table   | Content                                   | Status                 |
|---------|-------------------------------------------|------------------------|
| Table 1 | exact v7.13 gate definitions and outcomes | complete in Section 6  |
| Table 2 | Float64 crossing resolution               | complete in Section 7  |
| Table 3 | verification levels                       | complete in Section 5  |
| Table 4 | controlled file manifest                  | complete in Section 12 |

### 13.3 Machine-readable products

| Product                               | Status                       |
|---------------------------------------|------------------------------|
| terminal result JSON and solution NPZ | included and hashverified    |
| exact v7.13 gate and protocol JSON    | included and hashverified    |
| crossing-resolution JSON              | included and hashverified    |
| adjacent v6.74 NONPASS artifacts      | included and hashverified    |
| terminal checkpoint snapshot          | included and hashverified    |
| active runtime source path            | included and hashverified    |
| read-only verifier and manifest       | included; PASS               |
| AP1/AP2/AP3 templates                 | future work; no values exist |

## References

### Internal controlled sources

1. Apeiron - Start Here, latest persistent checkpoint.
2. Apeiron current project state, latest structured checkpoint.
3. Apeiron/AME-1 - Canonical Operational Model Specification, version 1.0.
4. Apeiron v7.13 - Exact Gate Specification, version 1.0.
5. Apeiron - Reproducibility Manifest and Read-only Verifier, version 1.0.
6. Apeiron/AME-1 Appendix A: Falsifiable Predictions - Guide for the Next Three Work Packages, version 1.0, 30 August 2026.

### External primary and official context

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These sources provide context only. They do not modify the internal Apeiron model or elevate AP1-AP3 to completed predictions.

# Part III - Publication gap report

German traffic-light audit and controlled resume point

## Apeiron - Publikationslückenbericht (Latest)

Version: 1.1-red-blockers-closed Stand: 30. August 2026 Geltung: erste venue-neutrale Grundlagenpublikation auf Basis des eingefrorenen v7.13-Rechenteils Gesamtstatus: frühere dokumentarische Blocker R-01 bis R-03 geschlossen; technischer Kern für kontrollierte Preprint-Paketierung geeignet; Journaleinreichung formal noch nicht vollständig

### 1. Gesamturteil

Der v7.13-HARD-PASS, der benachbarte v6.74-NONPASS und die Float64-Abbruchklassifikation sind exakt dokumentiert. Die früher fehlenden publikationskritischen Angaben wurden aus dem autoritativen Latest-Runtime-Pfad und den unveränderlichen Artefakten erschlossen, ohne Solverausführung und ohne Neuberechnung:

- operationale homogene Modellgleichungen, Einheiten, Freiheitsgrade, Parameter und diskrete Abbildung;
- exakte v7.13-Gates, Schwellen, Operatoren und Solverbudgets;
- einzeln hashgebundene Resultat-, Zustands-, Protokoll-, Crossing- und aktive Quelldateien;
- read-only Verifier mit PASS.

Damit sind R-01 bis R-03 als Dokumentationsblocker geschlossen. Nicht geschlossen sind Wirkungsfundierung, Kontinuumskonvergenz, Störungen, unabhängige numerische Reproduktion und empirische Prüfung. Diese Punkte begrenzen die wissenschaftliche Reichweite, machen den engen Bericht über die eingefrorene numerische Klassifikation aber nicht automatisch unpublishierbar.

### 2. Ampelregister

#### Grün - veröffentlichungsfähig und belegt

| ID   | Punkt                                               | Beleg / Ergebnis                                  | Publikationshandlung                                                                       |
|------|-----------------------------------------------------|---------------------------------------------------|--------------------------------------------------------------------------------------------|
| G-01 | terminaler v7.13-HARD-PASS                          | U1/U3/G1; Claims C-010-C-020                      | Werte, exakte Schwellen und Klassifikation dürfen repräsentationsbezogen berichtet werden. |
| G-02 | v6.74-NONPASS-Gegenendpunkt                         | U6; Claims C-021/C-022                            | nur mit seiner eigenen unveränderlichen Gate-Klassifikation berichten.                     |
| G-03 | Float64-Crossing                                    | U5; V1 PASS; Claims C-023/C-024                   | als Abschluss der gefrorenen binären Suche, nicht als physikalische Naturgrenze.           |
| G-04 | operationale Modelloffenlegung                      | S1; aktive Quellen in M1                          | homogene Gleichungen, Einheiten, Parameter, Zustand und diskrete Abbildung publizierbar.   |
| G-05 | exakte v7.13-Gate-Tabelle                           | G1; U3/U4                                         | im Haupttext und maschinenlesbar vollständig enthalten.                                    |
| G-06 | hashgebundene Reproduzierbarkeitsstufe V2.5         | M1; V1 PASS; README                               | als read-only Integritäts- und Konsistenzprüfung bezeichnen.                               |
| G-07 | Trennung von Numerik, Physik, Empirie und Ontologie | Claims-Register Abs. 5-6                          | in Abstract, Interpretation und Schluss beibehalten.                                       |
| G-08 | AP1-AP3 als Folgeprogramm                           | A1; Claims C-040-C-046                            | ausschließlich prospektiv; keine Kurven oder Mess-PASS.                                    |
| G-09 | venue-neutrales Mastermanuskript                    | APEIRON_MANUSCRIPT_L ATEST.md, Abs. 1-13          | technische Kernstruktur vollständig.                                                       |
| G-10 | Terminologie-Audit                                  | Claims-Register; konservativer Manuskriptwortlaut | starke Begriffe nur technisch eingegrenzt oder negiert.                                    |

## Gelb - redaktionell oder formal noch zu bearbeiten

| ID   | Punkt                                                                   | Risiko                                                           | Nächste Handlung                                                          |
|------|-------------------------------------------------------------------------|------------------------------------------------------------------|---------------------------------------------------------------------------|
| Y-01 | Zielformat und Zielzeitschrift                                          | unterschiedliche Format-, Umfangs- und Supplementregeln          | venue-neutral belassen, bis Entscheidung vorliegt.                        |
| Y-02 | Autoren, Zugehörigkeit und korrespondierende Person                     | Pflichtangaben fehlen                                            | nur autorisiert ergänzen; Platzhalter bis dahin beibehalten.              |
| Y-03 | CRedit, Finanzierung, Interessenkonflikte, Danksagung und KI-Disclosure | venue- und personenspezifisch                                    | vor Einreichung autorisiert ausfüllen.                                    |
| Y-04 | permanente Archivkennung und Lizenz                                     | öffentliche Dateiseite ist kein Ersatz für DOI/Repository-Lizenz | Zenodo, OSF oder institutionelles Archiv bei Freigabe wählen.             |
| Y-05 | Abbildungen                                                             | drei Figuren sind inhaltlich definiert, aber noch nicht gesetzt  | nur aus belegten Daten beziehungsweise als konzeptuelle Grafik erstellen. |
| Y-06 | Referenzstil und Literaturvollständigkeit                               | venue-abhängig                                                   | nach Journalwahl formatieren und finale Quellenprüfung durchführen.       |
| Y-07 | finale Sprachlektorat                                                   | englische Stil- und Symbolkonsistenz                             | nach inhaltlichem Freeze durchführen.                                     |
| Y-08 | Meilenstein-PDF                                                         | vorhandenes Dossier bildet den vorherigen Stand ab               | nach Paketabschluss neu erzeugen und visuell prüfen.                      |

## Orange - wissenschaftlich relevant, aber noch nicht ausreichend gestützt

| ID   | Punkt                                         | Warum orange                                           | Behandlung                                                                       |
|------|-----------------------------------------------|--------------------------------------------------------|----------------------------------------------------------------------------------|
| O-01 | fundamentale covariante Wirkung               | S1 definiert das Modell operational, nicht fundamental | als Grenze nennen; für diese enge numerische Publikation keine Wirkung erfinden. |
| O-02 | Kontinuums-/Gitterkonvergenz                  | nicht durch Latest-Evidenz belegt                      | Scope auf die eingefrorene Diskretisierung begrenzen.                            |
| O-03 | unabhängige numerische Reproduktion           | V1 prüft Dateien, rechnet aber nicht neu               | zukünftige externe oder clean-room Reproduktion.                                 |
| O-04 | globale und nichtlineare Stabilität           | terminale lokale Gates reichen nicht                   | ausdrücklich nicht beanspruchen.                                                 |
| O-05 | eindeutiges physikalisches Mapping von $\tau$ | in A1 als AP1-Aufgabe offen                            | kein Mapping zu $z$ oder $a$ erfinden.                                           |
| O-06 | lineare Störungen und Observable-Kurven       | noch nicht geschlossen hergeleitet                     | AP1; nicht Teil des HARD_PASS.                                                   |
| O-07 | AP2-Filamentprofil                            | offene Hypothese                                       | Folgearbeit mit Materierekonstruktion und Nulltests.                             |
| O-08 | AP3-GW-Propagation                            | Tensorsektor noch nicht hergeleitet                    | Folgearbeit; $c_{GW} = c$ als harte Bedingung.                                   |
| O-09 | vollständige physikalische Plausibilität      | Vergleich mit allen etablierten Grenzen fehlt          | keine Gesamtbestätigung behaupten.                                               |

## Rot - unzulässige Aussage

Die früheren R-01 bis R-03 sind geschlossen und werden nicht mehr als Rot geführt. Verbleibende rote Punkte sind Aussagen, die nicht durch redaktionelle Nacharbeit gerettet werden dürfen.

| ID   | Punkt                                                               | Art                     | Konservative Entscheidung                                      |
|------|---------------------------------------------------------------------|-------------------------|----------------------------------------------------------------|
| R-04 | "Apeiron ist empirisch bestätigt, bewiesen oder nachgewiesen"       | unzulässige Überaussage | vollständig ausschließen.                                      |
| R-05 | "Der Float64-Endpunkt ist die exakte physikalische Übergangsgrenze" | unzulässige Überaussage | nur repräsentationsabhängige Klassifikationsklammer behaupten. |
| R-06 | erfundene AP1-AP3-Kurven, Signifikanzen oder Mess-PASS              | Daten-/Ergebnisfiktion  | vollständig ausschließen.                                      |

| ID   | Punkt                                                                                                                       | Art                              | Konservative Entscheidung                                         |
|------|-----------------------------------------------------------------------------------------------------------------------------|----------------------------------|-------------------------------------------------------------------|
| R-07 | Genesis, ewiger Kreislauf, reale Apeiron-Filamente oder Schwarze Löcher als Apeiron-Fenster als Ergebnis dieses Rechenteils | unbelegte Scope-Ausweitung       | im aktuellen Manuskript nicht als Ergebnis führen.                |
| R-08 | “vollständig unabhängig reproduziert”                                                                                       | unzutreffende Methodenbehauptung | read-only Integritätsprüfung klar von Neuberechnung trennen.      |
| R-09 | “fundamentale covariante Wirkung bewiesen”                                                                                  | unzutreffende Modellbehauptung   | operationale Spezifikation nicht als Wirkungsherleitung ausgeben. |

### 3. Publikationsfähigkeit nach Aussageebene

| Ebene                               | Status             | Urteil                                                                                           |
|-------------------------------------|--------------------|--------------------------------------------------------------------------------------------------|
| technische Artefaktintegrität       | Grün               | Hashes, Identitäten, Formen und gespeicherte Gatevergleiche bestehen V1.                         |
| operationale Reproduzierbarkeit     | Grün               | Gleichungen, Parameter, Diskretisierung, Gates, Artefakte und aktiver Quellpfad sind paketiert.  |
| unabhängige numerische Reproduktion | Orange             | keine neue Ausführung; bewusst nicht behauptet.                                                  |
| interne numerische Modellkonsistenz | Grün, eng begrenzt | v7.13 erfüllt die exakten Gates der gefrorenen Diskretisierung.                                  |
| fundamentale Modellvollständigkeit  | Orange             | keine eindeutige covariante Wirkung oder Störungstheorie.                                        |
| physikalische Plausibilität         | Orange             | zusätzliche Theorie- und Vergleichsarbeit nötig.                                                 |
| empirische Bestätigung              | keine              | AP1-AP3 sind prospektiv.                                                                         |
| ontologische Interpretation         | Hypothese          | aus dem Rechenteil nicht ableitbar.                                                              |
| Preprint-Paketierung                | Grün/Gelb          | technischer Kern vorhanden; Autoren-, Lizenz-, Archiv- und Layoutangaben offen.                  |
| Journaleinreichung                  | Gelb               | keine roten technischen Dokumentationsblocker mehr, aber Pflichtangaben und Venue-Format fehlen. |

### 4. Abschluss der früheren roten Blocker

| früherer Blocker                                           | Abschlussartefakt                                        | Abschlussprüfung                                                                   |
|------------------------------------------------------------|----------------------------------------------------------|------------------------------------------------------------------------------------|
| R-01: Gleichungen, Freiheitsgrade, Einheiten, Konventionen | APEIRON_CANONICAL_MODEL_SPECIFICATION_LA TEST.md         | gegen den aktiven hashgebundenen Runtime-Pfad dokumentiert; keine Wirkung erfunden |
| R-02: exakte Gates und Toleranzen                          | APEIRON_V7_13_GATE_SPECIFICATION_LATEST.js on            | Identität von Protokoll- und Registerschwellen geprüft                             |
| R-03: einzeln auflösbare Artefakte und Verifikationsweg    | Manifest, technische Quellen, README, read-only Verifier | APEIRON_PUBLICATION_PACKAGE_VERIFY_PASS                                            |

### 5. Nächste grüne oder gelbe Aufgabe

Y-04 ist auf Paketebene abgearbeitet: APEIRON\_PUBLICATION\_REPRODUCIBILITY\_PACKAGE\_LATEST.zip wurde mit SHA-256 801f19dc26808184ccf4dfa33dd5429831c42fdb40b2048d16fd7c50b6ae0ac2 erstellt, der ZIP-Strukturtest bestand, und der aus einer temporären Entpackung gestartete read-only Verifier meldete PASS. Offen bleibt nur die spätere Wahl eines permanenten DOI-Archivs und einer Lizenz.

Als nächste gelbe Aufgabe folgt Y-08: Aktualisierung des Meilenstein-PDFs und visuelle Prüfung. Danach werden Meta, beide Latest-Handoffs und die öffentliche Dateiseite konsistent fortgeschrieben.

# Part IV - Canonical operational model specification

Frozen homogeneous equations, variables, units, parameters, and active-source hashes

## Apeiron/AME-1 - Canonical Operational Model Specification

Version: 1.0 Status: frozen technical supplement for the first numerical-foundations publication Date: 2026-08-30 Authority: active execution path in APEIRON\_FAST\_RUNTIME\_LATEST.zip, Library version 53, SHA-256 9b0d9212250a6b475b9a56647d0b34f7d8f87c0912c1ec9c004530a674951985

### 1. Scope and epistemic boundary

This is the canonical operational definition of the homogeneous model that produced the frozen v7.13 classification. It specifies variables, pressure function, background equations, quantum-source closure, discrete fixed-point map, initial data, units and conventions.

It does not assert a unique fundamental covariant action, perturbation theory, ontology or empirical confirmation. For the narrowly scoped numerical-foundations paper, the equations and executable map below are authoritative. An action-level completion would be new physics and cannot be projected backward onto v7.13.

### 2. Units, geometry and time

- Natural units:  $c = \hbar = 1$ .
- Reduced Planck mass as internal mass unit:  $M_{\text{pl}} = 1$ .
- Spatially flat homogeneous FRW background, scale factor  $a$ , e-fold variable  $N = \ln(a)$ , expanding branch  $H > 0$ .
- A dot denotes differentiation with respect to cosmic time  $t$ .
- Dimensionless numerical time:

$$\tau = H_{\text{star}} t \, d/d\tau = (1/H_{\text{star}}) \, d/dt$$

- Noncanonical kinetic scalar:

$$X = 0.5 (\dot{\theta})^2$$

- Scalar fields and mass parameters have mass dimension one.  $X$ , pressure and energy density have mass dimension four.

The operational sign convention is fixed by the equations below. A metric-signature convention not used explicitly by the homogeneous implementation is not added here.

### 3. Degrees of freedom and stored state

#### 3.1 Homogeneous state

The full eight-column trajectory container is

$$y(\tau) = (\sigma, \dot{\sigma}, \theta, \dot{\theta}, \chi, \dot{\chi}, H, N).$$

In the registered v7.13 map the homogeneous bookkeeping coordinate  $\chi$  is fixed to zero. The dynamically iterated six-column state is

$$u(\tau) = (\sigma, \dot{\sigma}, \theta, \dot{\theta}, H, N).$$

The  $\chi$  sector enters through the renormalized mode expectation values  $\rho_q(\tau)$ ,  $p_q(\tau)$  and  $\langle \chi^2 \rangle_q(\tau)$ , not through an independently iterated homogeneous  $\chi$ .

3.2 Discrete vector

The frozen grid has  $N_\tau = 15361$  nodes. The solver vector is the flattened and scaled array  $x = \text{vec}[ \sigma/(1e-2), \text{dot } \sigma/(1e-8), \theta/1, \text{dot } \theta/(1e-8), H/(1e-6), N/(1e-1) ]$  with shape (92166,) and Float64 dtype.

| Array | Shape      | dtype   | Meaning                             |
|-------|------------|---------|-------------------------------------|
| t     | (15361,)   | Float64 | dimensionless $\tau$ grid           |
| y     | (15361, 8) | Float64 | full trajectory container           |
| x     | (92166,)   | Float64 | scaled flattened six-column iterate |
| tau   | scalar     | Float64 | active terminal value               |

During unpacking, first-node  $\sigma$ , dot  $\sigma$ ,  $\theta$ , dot  $\theta$  and  $N$  are reset to the frozen background initial data. First-node  $H$  remains in the active state; the image map then imposes the positive Friedmann closure.

3.3 Auxiliary and constrained quantities

- $H$  is algebraically reconstructed from the positive Friedmann branch inside the registered image map.
- $N$  obeys dot  $N = H$ .
- Quantum modes and Pauli-Villars regulator sectors are auxiliary arrays used to construct  $p_q$ ,  $p_q$  and  $\langle \chi^2 \rangle_q$ ; they are not independent entries of  $x$ .
- Gate diagnostics are not additional dynamical degrees of freedom.

4. Frozen parameters

4.1 AME parameters

| Symbol                   | Value      | Code name |
|--------------------------|------------|-----------|
| $M_{pl}$                 | 1          | Mpl       |
| $\Lambda$                | $2.3e-3$   | Lambda    |
| $f_\sigma$               | $2.5e-2$   | f_sigma   |
| $E_c / V_{star}$         | $4.0e-2$   | Ec_over_V |
| $H_{star}$               | $2.0e-6$   | Hstar     |
| $b_{star}$               | 0.35       | bstar     |
| $d b / d(\theta/M_{pl})$ | $-4.78e-2$ | b_slope   |
| $A_{eff}$                | $6.86e-3$  | Aeff      |
| $B_{eff}$                | $-1.74e-2$ | Beff      |

$V_{star} = 3 M_{pl}^2 H_{star}^2 E_c = 0.04 V_{star}$

$A_{eff}$  and  $B_{eff}$  remain in parameter provenance; the active global pressure completion in Section 5 is the quartic polynomial  $V_s(\theta)$ .

## 4.2 Portal and regulator parameters

| Quantity                               | Value                       |
|----------------------------------------|-----------------------------|
| phase scale $f_{\text{phase}}$         | 0.8549468502440697          |
| displacement $v$                       | 0.03272387838931097         |
| coupling $\lambda$                     | 1.6740193604000272e-5       |
| bare portal mass $m_{\chi,0}$          | 9.817951142008693e-5        |
| physical-mode support at initial slice | $0 \leq k \leq 0.6 \Lambda$ |
| physical quadrature nodes              | 128                         |
| renormalization scale                  | $\mu_R = 1.5 \Lambda$       |
| UV order-0 switch                      | 16 $\Lambda$                |
| curvature-tail limit                   | 64 $\Lambda$                |
| tail nodes per octave                  | 20                          |

## 5. Effective AME pressure and derivatives

Define

$$z = \sigma/f_{\sigma} \quad b(X, \theta) = b_{\text{star}} + b_{\text{slope}} (\theta/M_{\text{pl}}) - 5X/\Lambda^4 \quad F(z, b) = z^4/4 - z^2/2 + bz \quad V_s(\theta) = \sum_{i=0..4} c_i \theta^i$$

with

$$(c_0, c_1, c_2, c_3, c_4) = (1.1971212004620583e-11, 9.87022611239063e-14, -1.0336424891583054e-13, 1.189490499106138e-10, 1.2236365189926054e-10)$$

The homogeneous pressure function is

$$P(X, \sigma, \theta) = X + [5/(3\Lambda^4)] (z - 2/\sqrt{3})^2 X^2$$

- $E_c F(z, b)$
- $V_s(\theta)$ .

The executable derivatives are

$$P_X = 1 + [10/(3\Lambda^4)] (z - 2/\sqrt{3})^2 X + 5 E_c z/\Lambda^4$$

$$P_{XX} = [10/(3\Lambda^4)] (z - 2/\sqrt{3})^2$$

$$P_{\sigma} = \{ [10/(3\Lambda^4)] (z - 2/\sqrt{3}) X^2$$

- $E_c (z^3 - z + b) / f_{\sigma}$

$$P_{\theta} = -E_c z b_{\text{slope}}/M_{\text{pl}} - V_s'(\theta)$$

$$P_{X\sigma} = \{ [20/(3\Lambda^4)] (z - 2/\sqrt{3}) X + 5 E_c/\Lambda^4 / f_{\sigma}.$$

AME stress:

$$\rho_{\text{AME}} = 0.5 (\dot{\sigma})^2 + 2X P_X - P \quad p_{\text{AME}} = 0.5 (\dot{\sigma})^2 + P.$$

Hyperbolicity diagnostics:

$$P_X > 0 \quad P_X + 2X P_{XX} > 0.$$

## 6. Portal and quantum source

Field-dependent portal mass:

$$m_{\chi^2}(\sigma, \theta) = m_{\chi,0}^2 + 2\lambda(v+\sigma)^2 \cos(2\theta/f_{\text{phase}})$$

$$\partial m_{\chi^2}/\partial \sigma = 4\lambda(v+\sigma) \cos(2\theta/f_{\text{phase}})$$

$$\partial m_{\chi^2}/\partial \theta = -[4\lambda(v+\sigma)^2/f_{\text{phase}}] \sin(2\theta/f_{\text{phase}}).$$

Four Pauli-Villars sectors:

$$C_j = (1, -3, 3, -1) \quad J_j = (0, 1, 2, 3) \quad M_j^2 = m_{\chi^2} + J_j \mu_R^2.$$

Modes are advanced by a three-substep Yoshida composition of the implicit-midpoint map for  $u = a^{(3/2)} \chi$ . Initial mode data are

$$u_k(0) = 1/\sqrt{2\omega_k(0)} \dot{u}_k(0) = -i \omega_k(0) u_k(0).$$

The active source combines resolved modes, the analytic order-0 UV tail and auxiliary adiabatic curvature orders 2 and 4. Finite renormalization is fixed on the initial flat-space reference slice as recorded by the active runtime:

- $\rho_q(0) = 0$ ;
- $\langle \chi^2 \rangle_q(0) = 0$ ;
- initial quantum pressure is predicted by the fixed prescription rather than tuned as a gate;
- the Einstein-Hilbert response is fixed by the zero-curvature response;
- the finite  $R^2$  coefficient is zero.

The routine returns  $\rho_q(\tau)$ ,  $p_q(\tau)$  and  $\langle \chi^2 \rangle_q(\tau)$ . Its source identity is

$$\dot{\rho}_q + 3H(\rho_q + p_q)$$

- $0.5 (\dot{m}_{\chi^2}) \langle \chi^2 \rangle_q = 0$ ,

evaluated as a normalized numerical diagnostic.

## 7. Registered homogeneous equations

With

$$\rho_{\text{tot}} = \rho_{\text{AME}} + \rho_q \quad p_{\text{tot}} = p_{\text{AME}} + p_q,$$

the registered image map integrates

$$d\sigma/dt = v_\sigma$$

$$dv_\sigma/dt = -3H v_\sigma + P_\sigma$$

- $0.5 (\partial m_{\chi^2}/\partial \sigma) \langle \chi^2 \rangle_q$

$$d\theta/dt = v_\theta$$

$$dv_\theta/dt = \{ P_\theta$$

- $0.5 (\partial m_{\chi^2}/\partial \theta) \langle \chi^2 \rangle_q$
- $3H P_X v_\theta$
- $P_X \sigma v_\sigma v_\theta$

$$/ (P_X + 2X P_{XX})$$

$$H = +\sqrt{[\rho_{\text{tot}}/(3 M_{\text{pl}}^2)]}$$

$$dN/dt = H.$$

The Raychaudhuri relation

$$dH/dt = -(\rho_{\text{tot}} + p_{\text{tot}})/(2 M_{\text{pl}}^2)$$

is evaluated independently rather than used as the evolution equation in this image map.

## 8. Initial data

$$\theta(0) = -0.690 \quad \varepsilon_0 = 2.35e-5 \quad N(0) = 0$$

$$\dot{\theta}(0) = -\sqrt{2 \varepsilon_0} M_{\text{pl}} H_{\text{star}} / \sqrt{1.3}$$

$$\dot{\sigma}(0) = 0.$$

$\sigma(0) = f_\sigma z_+$ , where  $z_+$  is the positive local minimum satisfying

$$z^3 - z + b(\theta(0)) = 0 \quad 3z^2 - 1 > 0.$$

The initial Hubble value is the positive Friedmann root. Homogeneous portal bookkeeping data are  $\chi(0) = \dot{\chi}(0) = 0$ . No spatial boundary conditions occur because the registered model is homogeneous.

## 9. Canonical discrete fixed-point map

For active endpoint  $\tau_{\text{end}}$ ,

$$\Delta\tau = \tau_{\text{end}} / 15360.$$

The canonical image map  $G(x;\tau_{\text{end}})$ :

1. creates the uniform 15361-node  $\tau$  grid and frozen background seed;
2. unpacks  $x$  into the six active trajectory columns using Section 3.2;
3. imposes frozen first-node conditions;
4. calculates renormalized quantum-source arrays with the fixed portal and PV prescription;
5. advances  $(\sigma, \text{dot } \sigma, \theta, \text{dot } \theta, N)$  by classical fourth-order Runge-Kutta while imposing the positive Friedmann root for  $H$ ;
6. lifts the result to the eight-column container and repacks the six active columns.

Residual and fixed-point diagnostic:

$$R(x;\tau) = x - G(x;\tau) \quad \delta_{\text{FP}} = ||R||_{\text{infinity}}.$$

This is complete for the frozen homogeneous discrete map. It does not license continuum, perturbative, global-stability or observational claims.

## 10. Active-source provenance

| Source file                               | SHA-256                                                          | Role                                           |
|-------------------------------------------|------------------------------------------------------------------|------------------------------------------------|
| model.py                                  | db4c0fa9cf4f2013fef299f558ca7b6b509d17c1acbd76f84ece6bd2dd0c5a65 | parameters and pressure primitives             |
| frw_noncanonical_backgrou<br>nd_v6_6.py   | f96b13df83e6d6dce8f9bec073e2aab24c23660073cee994d25a327f2b61f7f1 | homogeneous equations and initial data         |
| frw_pv_fixed_mpl_renorm_v<br>6_17.py      | aecd4dc3202604228d1a46c1a4cb439b874e129314e55378e1fbb5b999df482d | stress tensor, renormalization and diagnostics |
| frw_pv_covariant_uv_comple<br>te_v6_22.py | 9c54b4095845687b9824dab66da91031436b67a5decd01055ef487b14b4c19b7 | UV-tail closure                                |
| frw_pv_uv_yoshida_v6_31.py                | 8fa1b93a2f24377c751f3d9fdffe700394cdb2e00842fc4dc5f35d19ae3943e1 | registered mode evolution                      |
| rb19_anderson_uv_v6_24.py                 | 8323bbf6c6f3e23e1d466addf5cceb94af2517934fddd50ce8fcef4ae04fcc2c | state packing                                  |
| rb23_friedmann_closure_uv_<br>v6_28.py    | 873d3eca436d28b4261623957917087b0dd2efdf3b95509b9fb97d1fe4f5d7bc | Friedmann map and Raychaudhuri audit           |
| rb_recovery_fixedtau_v6_64.<br>py         | 5082e44cf9c60ca9ef1eaa0ba1ccda7d968d19f61ea1d3d2e9c7581be82ee72b | fixed-point and solver base                    |
| rb_recovery_adaptive_v7_13.<br>py         | 8854c5847f9da3e67994701a20e8f4f6e9372c0a65da3f2f3ea0fd7017f81205 | v7.13 wrapper and schedule                     |

Filename version labels record dependency origin. They appear only because these files form the active hash-frozen execution path of the Latest runtime. No alternative historical model is reconstructed.

## 11. Licensed publication statement

Maximum supported wording:

> Apeiron/AME-1 v7.13 is a frozen homogeneous FRW numerical model defined operationally by the equations, parameters, state map, quantum closure, discretization and hash-identified active runtime sources in this supplement.

Inadmissible stronger wording:

> The supplement proves a unique fundamental or covariant theory of Apeiron.

## Part V - Read-only reproducibility guide

Package scope, verification command, and epistemic boundary

# Apeiron v7.13 - Read-only Reproducibility Package

## Scope

This package verifies the integrity and documentary consistency of the frozen v7.13 terminal result and the adjacent v6.74 NONPASS endpoint. It does not start a solver, evaluate the physical map, repeat the crossing search, or alter any state.

## Run

```
python3 verify_apeiron_publication_package.py
```

Expected terminal line:

```
APEIRON_PUBLICATION_PACKAGE_VERIFY_PASS
```

## Verification levels

1. SHA-256 verification of every registered artifact and active source.
2. JSON schema/key and cross-document identity checks.
3. NPZ key, shape, dtype, and stored- $\tau$  checks.
4. Documentary comparison of recorded diagnostics with the immutable threshold table.
5. Float64-adjacency plus exact protocol-decimal midpoint and recorded binary64-rounding checks.

No diagnostic is recomputed from the physical equations. The script only verifies the already recorded values and classifications.

## Environment

- Python 3.12.13
- NumPy 2.3.5
- SciPy is not required for this read-only verifier.

## Directory structure

- `APEIRON_CANONICAL_MODEL_SPECIFICATION_LATEST.md`: canonical operational equations and conventions.
- `APEIRON_V7_13_GATE_SPECIFICATION_LATEST.json`: exact v7.13 thresholds and rules.
- `APEIRON_REPRODUCIBILITY_MANIFEST_LATEST.json`: hash manifest.
- `TECHNICAL_SOURCES/`: immutable result, state, protocol, gate, crossing, and active-source files.
- `verify_apeiron_publication_package.py`: read-only integrity verifier.

## Scientific boundary

A successful verification confirms that the released files match the frozen documented package and that their recorded values are internally consistent. It is not an independent numerical reproduction, empirical validation, or ontological proof.